Design Considerations for Micro-Glassblown Atomic Vapor Cells

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Abstract—This paper presents a design process for miniaturized atomic vapor cells using the micro-glassblowing process. It discusses multiple design considerations, including cell geometry, optical properties, materials, and surface coating. The geometry and the optical properties were studied using experimentally verified analytical and Finite Element Models (FEM). The cell construction material and surface coating were the focus of our experimental study on factors that affect the relaxation time (T2) of nuclear spins. We showed that the wafer-level coating process with Al2O3 increased the 131Xe T2 by 3× and by switching from Borosilicate glass (Pyrex) to Aluminosilicate glass (ASG), T2 was improved by 2.5×, for the same species. The improvement in the T2 is projected to reduce the ARW of an NMR gyro and the sensitivity of an NMR magnetometer by 3× T2 is projected to reduce the ARW of an NMR gyro and the improved by 2.5×

Borosilicate glass (Pyrex) to Aluminosilicate glass (ASG), T2 was improved by 2.5×, for the same species. The improvement in the T2 is projected to reduce the ARW of an NMR gyro and the sensitivity of an NMR magnetometer by 3× with Al2O3 coated cells and by 2.5× with ASG cells. [2019-0158]

Index Terms—Glassblowing, atomic sensors, microfabrication, nuclear magnetic resonance (NMR), NMR gyroscopes, atomic cells, relaxation time.

I. INTRODUCTION

MINIATURIZATION of atomic vapor cells is a critical technology for chip-scale “hot” and “cold” atomic-microsystems. These microsystems include, but are not limited to, chip-scale magnetometers [2]–[4], clocks [5], and gyroscopes [4], [6], [7]. Some of the challenges in cells development that arise from miniaturization include development of: a batch fabrication process that yields small size, weight, power, and cost (SWAP+C) cells [8]; low SWAP+C cells with geometrical requirements such as multiple optical ports and cell symmetry; cells with homogeneous wall material; wall coatings and materials that preserve the atomic polarization inside the cells. Multiport cells are needed for applications such as Nuclear Magnetic Resonance (NMR) gyros and magnetometers, [9], [10], while symmetry is preferred for all atomic vapor cells to avoid unwanted phenomena, such as self-magnetization and quadrupole shift, [11]. In-homogeneity in the cell wall material increases cell asymmetry, [12], which increases quadrupole frequency shift that negatively affects the performance of NMR atomic sensors. Additionally, with miniaturization of atomic cells, the interaction of atomic vapor with the cell walls increases due to the increase of the surface area to volume ratio, [13]. This calls for a careful selection of cell materials and surface treatment processes.

The fabrication and filling of miniaturized-glassblown spherical cells, [1], [14]–[16], enabled a wafer-level fabrication of highly spherical axisymmetric multiport cells with homogeneous wall material that addressed some of cell design challenges. In this paper, we discuss design process considerations, which were not previously considered, including geometry, optical properties, materials, and surface treatment (coating). The design process combines analytical, [14], and finite element modeling (FEM) of the cell’s geometry and optical properties, [17], [18], that are backed up by experimental validation. In this paper, we also expand on our study of cell wall materials and surface coating.

This paper is structured as follows. In Section II, we briefly described the overall design approach of miniaturized cells. Then, in Section III, we discuss the geometrical aspect of the cell fabrication, where we introduced analytical and finite element models and, subsequently, supported results of analysis by experimental validation. In Section IV, we presented the optical modeling and simulation results of the fabricated cells backed up by experimental validation. Section V talks about a study of materials and cell wall coating on the performance of atomic cells. Section VI concludes the paper with an outlook on the spectrum of applications that can benefit from the presented design approach.

II. GLASSBLOWING PROCESS

Glassblowing of miniaturized cells on a wafer-level is based on anodic bonding a glass wafer to a silicon wafer with pre-etched cavities under atmospheric pressure conditions.
The wafer stack is then heated up to a temperature higher than the softening point of the glass; the combination of glass softening and pressure build-up in the pre-etched cavities creates axisymmetric spherical shells, Fig. 1, [14].

After the glassblowing step, the cells are rapidly cooled down to preserve their shape and to prevent any crystallization of the glass, [19]. This rapid cooling puts a thermal shock on the cell walls and builds up stresses across the geometry. Additionally, the cooling process results in a pressure drop inside the cells, which creates a pressure difference across the cell walls. Depending on the pressure difference and wall thickness, breakage might happen at the thinnest part of the cell.

For analysis, we use a multi-step approach for designing miniaturized glassblown cells. The design process starts with an analytical model presented in [14], which estimates dimensions of the resulting geometry of cells. Next, a finite element model predicts a more realistic geometry of the cell using isothermal flow simulation in COMSOL. The resulting geometry is then exported to solid mechanics simulation, which estimates the maximum stress on the cell walls and predicts whether the cell can survive the force generated by the pressure difference across its walls. Finally, the model is exported to optical simulation software to simulate the optical behavior of the cells.

III. Geometry

In this section, we present an analytical model and FEM model, and in light of the two models, we discuss the parameters that influence the geometry of the cells, such as their size, sphericity, and wall thickness. Subsequently, we present experimental characterization that validates the simulation results.

A. Analytical Model

The height \( h_g \) and the inner radius of the cell \( r_g \), shown in Fig. 1, are given by equations (1) and (2), respectively, [14]

\[
h_g = \frac{\left(3V_g + \sqrt{r_o^6 \pi^2 + 9V_g^2}\right)\pi^{2/3}}{\pi\left(3V_g + \sqrt{r_o^6 \pi^2 + 9V_g^2}\right)\pi^{1/3}} - r_o^2 \pi^2
\]

\[
r_g = \frac{h_g^2 + r_o^2}{2h_g}
\]

where \( V_g \) is the inner volume of the cell and is defined as

\[
V_g = h_e \pi r_o^2 \left(\frac{T_f}{T_s} - 1\right)
\]

where \( T_f \) and \( T_s \) are temperatures of the glassblowing furnace and the cavity sealing measured in Kelvins, \( P_f \) and \( P_s \) are the pressure values (in Torr, for example) during the glassblowing and the cavity sealing, respectively, \( r_o \) is the radius of the etched cavity and \( h_e \) is the etched cavity depth. The average thickness of the cell wall can be estimated as [14],

\[
\delta = \frac{\delta_0 r_o^2}{h_g^2 + r_o^2}
\]

where \( \delta_0 \) is the initial glass layer thickness, as shown in Fig. 1.

The glassblowing process parameters (\( r_o \) and \( h_e \)) can produce a wide variety of cell sizes and sphericity levels. Fig. 2 depicts a selected subset of these parameters. In this paper, our target application for the glassblown shells is miniaturized atomic cells, so a cell radius, \( r_g \), on the order of 1mm is desired. A range of the cavity radii \( r_o \), that produces a cell with \( r_g = 1\text{mm} \), is from 488\( \mu \text{m} \) to 945\( \mu \text{m} \). However, as it was noted in [14], a smaller \( r_o \) is recommended to achieve higher sphericity cells.

The increase in cell sphericity reduces its asymmetry. Cells with high asymmetry have shown larger quadrupole splitting in \( ^{131}\text{Xe} \) frequency, [11].

B. Sphericity

The cell sphericity is defined as the ratio of the effective volume to the surface area of the exposed part of the cell above the glass wafer surface level, [20]. It is calculated as

\[
\Psi = \frac{\pi^{1/3}(6V'_{g})^{2/3}}{A_g},
\]

where \( V'_{g} \) and \( A_g \) are the volume and the surface area of the exposed part of the cell, which is above the glass wafer surface.
level, and both are calculated as

\[ V' = \frac{\pi}{3} h g \exp (3r - h g \exp), \]

\[ A g = \pi h g \exp (4r - h g \exp), \]

where \( h g \exp \) is the height of the exposed part of the shell, defined as

\[ h g \exp = h g - \delta_0 \]

Note, \( h g \) is defined from the silicon /glass interface to the top of the cell, as shown in Fig. 1.

There are several approaches to produce cells with higher sphericity. These include controlling the process pressure, either by increasing the initial cavity pressure \((P_f)\), [21], or reducing the glassblowing furnace pressure \((P_f)\), [18], or both. Another approach is to increase the initial volume of the cavity while keeping the cavity radius \( r_o \) small, as it was suggested in [14]. In this process, a stack of two wafers was used to build the Si cavity. The first one is a thick Si wafer, 1mm for example, where large cavities are etched. The second wafer is a thin wafer, 100μm for example, bonded to the first wafer and smaller openings are etched through, Fig. 3. This approach allows for larger volume without sacrificing sphericity and relaxes the requirement on the depth of etching. The inner volume of the cell becomes

\[ V = [h_1 \pi r_c^3 + h_2 \pi r_e^2 \left( \frac{T_f P_s}{T_g P_f} - 1 \right)], \]

where \( h_1 \) and \( r_e \) are the cavity depth and radius of the wafer 1, and \( h_2 \) is the wafer 2 thickness.

To improve sphericity, one can reduce the glass thickness to increase the exposed part on top of the glass surface. However, that would create thin shells, and the pressure difference across the shell walls will create compressive stress that is larger than the compressive strength of the glass material, which would lead to breaking of the cell. To estimate the maximum cell volume, we created a finite element model, which is discussed next.

C. Finite Element Model

The glass wall thickness is not uniform in this process, [14], and since this parameter is essential to accurately predict the light interaction with the cell walls, we used a finite element model using COMSOL Fluid Flow physics to estimate the wall thickness distribution in addition to the maximum volume of the cells. The developed model was adopted from our previous work, [17]. The shape of the glassblown cell at different time steps is predicted with a Newtonian isothermal fluid flow model with an adaptive re-meshing in COMSOL Multiphysics FE Package. In this model, the instantaneous volume and pressure of the cell and the cavity were calculated at each time step of the simulation, and once the equilibrium-state is reached the deformation of the glass layer stops. Fig. 4 shows snapshots of initial and final geometry of cell’s cross-section during the glassblowing.

The resulting geometry from the fluid flow model was exported to a solid mechanics simulation, and the pressure difference after cooling was calculated and applied to the cell’s outer surface to estimate the maximum stress value and location. The model predicted that the maximum stress was always concentrated at the top part of the cell and that it is because the shell’s minimum thickness is at the top, which matches what was experimentally demonstrated earlier in [14].

D. Glass Thickness \( \delta_0 \)

Using a combination of the FEM model and compressive strength of the Borosilicate glass (100 MPa), we estimated the maximum cell volume that would survive the glassblowing process. This process was repeated for different ratios of the glass thickness \( \delta_0 \) to the cavity opening \( r_o \). Sphericity of the exposed part of the cell was calculated using equation (5). The trend in Fig. 5 shows that as we increase the glass thickness relative to the cavity radius, sphericity of the maximum cell size drops following closely a quadratic line equation

\[ f(x) = ax^2 + bx + c, \]

where, \( x \) represents a normalized glass thickness \( (\delta_0/r_o) \), and coefficients \( a, b \) and \( c \) are \(-2.55\pm2.14, -1.83\pm5, \) and \( 98.53\pm2.57, \) respectively, with 95% confidence bounds. Additionally, increasing the normalized glass thickness increases the thickness variation of the cell walls from top to bottom. On the other hand, the normalized radius (normalized radius is the radius of a three-point circle fitted to the top and two sides of the exposed part of the cell divided by the cavity opening \( r_o \)) of the maximum cell volume, that would survive
the glassblowing and the subsequent cooling, was found to increase quadratically with the increase of the glass thickness relative to the cavity radius $r_o$. The equation parameters of the curve fitting line in Fig. 6, $a$, $b$ and $c$ are $-0.29\pm0.16$, $1.98\pm0.4$, and $1.516\pm0.2$, respectively, with 95% confidence bounds.

From Fig. 5 we deduce that in order to achieve a high sphericity level, one should use a glass thickness, that is $1/10$th of the cavity radius $r_o$. From Fig. 6, $r_o$ should be on the order of $1.7\times$ of the desired cell radius $r_g$. For example, if a cell of radius 1mm is desired, the cavity opening radius $r_o$ should be $588\mu m$ and the glass thickness $d_0$ should be $\approx 59\mu m$, to achieve $\approx 98\%$ sphericity. From equation (4), the average thickness of the resulting shell will be $\approx 6.5\mu m$. While this combination of parameters would survive the pressure difference due to glassblowing, from a practical point of view, it might not survive other steps of the process, such as backside opening and subsequent wet cleaning.

**E. Characterization of Geometry**

To validate the model, we fabricated two samples on a 1mm thick wafer, and $350\mu m$ glass (Pyrex) thickness, the Si cavity radii for the samples were $225\mu m$ and $300\mu m$, while the etch depth was $700\mu m$. The measured cell radius and height of these cells are presented in Table I. Visual inspection shows that an agreement between the fabricated cell and the geometry predicted by the FEM simulation, in terms of the cell height and radius, is within 95%.

**IV. Optical Properties**

In this section, we present an optical simulation model and discuss optical properties of the glassblown cells. The optical properties of interest for the atomic cells are light transmission through the cell and variation in optical polarization. Both parameters are critical for designs of NMR sensors.

**A. Simulation**

The optical simulation was performed using Monte Carlo ray tracing method, [22]. In this method, the light beam is broken down to a large number of individual rays and the interaction of those rays with different parts of the miniaturized cell is then integrated using Monte Carlo integration to predict the behavior of the whole beam within the cell.

The simulation shows that due to the change of the cell wall thickness, different parts of the beam experience different diffraction angles. The bottom part of the cell is usually the thickest, which causes the beam at that section to diffract downward and be trapped in the cell, bundle “A” in Fig. 7-(top). The mid-section of the beam transmits through the cell; however, it still experiences downward bending, as it propagates out of the cell, bundle “B” in Fig. 7-(top). Additionally, the beam polarization was analyzed by grouping individual rays into pockets and averaging their polarization parameters (ellipticity and azimuth angle). The polarization maps in Fig. 8 show that the cell preserves the azimuth angle and ellipticity for the majority of the transmitted beam, Fig. 8-a) and Fig. 8-b), respectively, and the degree of polarization is within 95%. This polarization distortion is negligible and it does not affect the operation of sensors.

The simulation also shows that cells with small normalized glass thickness and high sphericity pass the light beam through with minimal diffraction, Fig. 7-(bottom).

**B. Optical Characterization**

We measured the optical properties of the fabricated samples, discussed in Section III-E. The experimental setup consisted of a laser beam, a linear polarizer, and a quarter wave plate, creating a circularly polarized light that enters the sample. The transmitted light then propagates to a polarimeter (Thorlabs PAX 5710). The power and polarization of the optical beam were measured before and after the transmission through the samples. The beam radius was $\approx 0.5\times$ of the cell

**TABLE I**

Comparison between simulated and experimentally measured parameters of two fabricated samples, (all measurements are in (mm))

<table>
<thead>
<tr>
<th></th>
<th>Simulation Radius</th>
<th>Experiment Radius</th>
<th>Simulation Height</th>
<th>Experiment Height</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cell 1</td>
<td>0.78</td>
<td>0.79</td>
<td>1.33</td>
<td>1.34</td>
</tr>
<tr>
<td>Cell 2</td>
<td>0.93</td>
<td>0.98</td>
<td>1.67</td>
<td>1.71</td>
</tr>
</tbody>
</table>
radius. Table II shows a comparison between the measured and simulated optical transmission and polarization of the two fabricated samples. The simulation results are consistent with the well-known 4% per surface loss at an air/glass interface. The discrepancy between the measured and simulated values can be a result of the parasitic glass bubbles on the samples due to defects that could have blocked a part of the transmitted light and changed its polarization.

As mentioned earlier, micro-glassblown cells have multiple in-plane and out-of-plane ports. Even though in-plane ports provide optical paths for light transmission through the cell, the cells are not perfectly symmetric around them, and the beam would experience a downward bending, as discussed earlier. On the other hand, the cells are axisymmetric around the out-of-plane port, but their transmission is limited by the glassblowing cavity opening \( r_g \), which is on the order of \( 1/2 \) of the cell radius \( r_c \). To estimate the optimal orientation of light coupling to atomic sensors, we used the optical magnetometer scale factor as a metric to compare different orientations. The first configuration is in-plane (horizontal) pumping and probing, Fig. 9-(a); the second configuration is out-of-plane (vertical) pumping and horizontal probing, 9-b).

Fig. 10 shows the Rubidium magnetometer response of the two configurations; the vertical pumping improved the magnetometer scale factor by \( 2 \times \).

V. FILLING AND COATING

In this section, the filling and coating process of miniaturized spherical atomic cells are discussed. We briefly introduce the fabrication and filling process followed by a study on different wall materials and coating and experimentally measured their effect on the nuclear spins relaxation.

A. Background

The transverse relaxation time of the noble gas atoms is directly related to the performance of NMR sensors. For gyroscopes, for example, the angle random walk (ARW) is
predicted to depend on $T_2$ time as follows, [23],
\[
ARW = \frac{3600}{T_2 \times SNR \sqrt{\delta f}} \left[\frac{\circ}{\sqrt{\text{hr}}}\right], \tag{11}
\]
where $T_2$ is the transverse relaxation time of the Xe atoms, SNR is the signal-to-noise ratio of the electron paramagnetic resonance (EPR) magnetometer, and $\delta f$ is bandwidth of the phase noise in Hz. The fundamental sensitivity limit of an NMR magnetometer (NMRM) depends on the $T_2$ time as, [10],
\[
\delta B_n \leq \frac{1}{2\pi \gamma T_2} \times \frac{\delta B_e}{P \times dB_n/dP}, \tag{12}
\]
where $\delta B_e$ is the noise floor of the EPR magnetometer, $P$ is the percentage of polarized Xe atoms, $dB_n/dP$ is the magnetic field produced by Xe atoms per unit polarization, taking into consideration the “enhancement factor” of direct interaction with the alkali metal vapor, [24]. Several factors can affect the relaxation time of the noble gas atoms in atomic vapor cells, summarized as, [25], [26],
\[
\frac{1}{T_{2\text{[total]}}} = \frac{1}{T_{2\text{[coll]}}} + \frac{1}{T_2} + \frac{1}{T_{2\text{|AB}}} + \frac{1}{T_{2\text{|wall}}}, \tag{13}
\]
where, $T_{2\text{[total]}}$ is the effective transverse relaxation time, $T_{2\text{[coll]}}$ is the relaxation time due to collisions with alkali metal atoms, $T_2$ is the relaxation time due to self-collision of Xe atoms, $T_{2\text{|AB}}$ is the relaxation time due to magnetic field inhomogeneity inside the cell, and $T_{2\text{|wall}}$ is the relaxation time due to collisions of atoms with cell walls. In mm-sized cells, the wall collisions and spin exchange relaxation are dominant, [13], and therefore special care needs to be taken during the cell construction.

**B. Fabrication and Filling Process**

There are multiple filling approaches to introduce alkali metal and buffer gas in the miniaturized cells. The approaches have been discussed widely throughout the literature, [27]–[34]. The approach that we adopted in this paper for filling cells using an on-chip alkali metal dispenser was introduced previously for planar cells in [35] and [36]. A recent study that reviewed those approaches for atomic clocks, [37], comes to the conclusion that a filling process like the one suggested here, which combines an on-chip dispensing alkali source with high-temperature anodic bonding, has excellent MEMS compatibility, internal atmosphere quality, and process repeatability.

The fabrication process starts by etching 700 µm cavities in a 1 mm thick Si wafer, Fig. 11-(a). Next, the first anodic bonding seals the etched cavities under atmospheric pressure, Fig. 11-(b). After placing the wafer stack in a high-temperature furnace at 850 °C for Borosilicate glass (Pyrex) and 1000 °C for Alumino-silicate glass (ASG) for 5-7 minutes, spherically shaped glass shells are formed, [14], Fig. 11-(c). The formation was due to two effects: the trapped air inside the cavities builds up the pressure due to the temperature increase, and the glass transitions from a solid state to a viscous state.

The next steps in the process are to open the backside of Si wafer and to define 100 µm deep micro-channels using Deep Reactive Ion Etching (DRIE), Fig. 11-(d). Subsequently, the cell coating was applied via atomic layer deposition (ALD) of 10 nm aluminum oxide (Al$_2$O$_3$) to the opened cells and the capping wafer, Fig. 11-(e).

The second anodic bonding took place after the alkali dispenser pills have been placed in the central cell, with the ALD Al$_2$O$_3$ as an intermediate layer between the backside of the Si wafer and the capping glass wafer, Fig. 11-(f). The wafer alignment for bonding was performed inside a chamber with a noble gas and a buffer gas at pressures of 250-350 Torr, Fig. 11-(f). After the bonding process was complete, each dispenser was activated by focusing a 3.5-4W laser for 15 seconds, which released the alkali vapor to satellite cells, Fig. 11-(g).

**C. Design of Experiment**

The study aims to test the effects of different materials and surface coatings on relaxation time of Xe atoms by isolating all factors that affect the relaxation, except for the effect of wall interactions. Three samples were fabricated. The first (PXE01) was fabricated using Borosilicate glass (Pyrex) and was utilized as a baseline in our study; the second (PAXE01) was made with Pyrex and coated using Atomic Layer Deposition (ALD) of 10nm Aluminum Oxide (Al$_2$O$_3$); the third (HXE02) was fabricated using Alumino-silicate glass (ASG). To isolate other factors beside cell walls, the samples were filled with similar amounts of noble and buffer gases, and were tested under the same conditions of temperature and
Fig. 11. Description of the process flow: (a) DRIE etching of 700μm and through wafer cavities in 1mm Si wafer, (b) first anodic bonding of glass to the etched Si wafer, (c) glassblowing of cells, (d) cell back-side opening and channel definition using DRIE etching, (e) Atomic Layer Deposition (ALD) of 10nm Al₂O₃, (f) loading the Rb dispenser and performing the second anodic bonding in a noble gas and buffer gas filled chamber, (c) dispensing alkali metal through micro channels by laser heating of Rb source.

Fig. 12. Measured Rb absorption curve for the reference cell (blue) shows multiple distinguishable absorption peaks. Measured absorption of a micro cell (green), the cell was filled with 300 Torr of only N₂ and Rb, which broadened and shifted the peaks. In curve fitting to the micro cell spectrum (dashed red), the width of the curve represents 95% confidence bounds, which confirmed a close fit to the experimentally measured data.

Fig. 13. Top: Dual beam optical setup for characterization of cells. (LP: linear polarizer, QWP: quarter wave plate, PBS: polarizing beam splitter, PD: photo detector, Faraday Detector: a balanced polarimeter used to detect Faraday rotation). Bottom: Picture of the experimental setup showing the pump, probe, and the heating laser beams, as well as the nested magnetic shields and the cell oven.

magnetic field levels. Optical heating was used to minimize any interference from resistive heaters.

The pressure values at room temperature were: 65 Torr, 45 Torr and 300 Torr for natural Xe, Ne, and N₂, respectively. A data fitting of the Rb absorption curve (obtained by sweeping the wavelength of the VCSEL beam passing through the cell) was used to confirm the amount of noble and buffer gasses inside the cell. Measurements showed a reduction of the N₂ gas pressure by 20%-30%, which was attributed to absorption by the getter material in the Rb pill. The experimentally measured relaxation time (T₂) of ¹²⁹Xe and ¹³¹Xe isotopes were used to compare cells. The cells were heated optically using a 2.5W laser source at 1550nm, focusing only on the Si part of the cell substrate. We used the free induction decay (FID) method to estimate the relaxation rate using a dual beam scheme, one for pumping and another for detection, Fig. 13. The FID experiment was performed by applying a static magnetic field B₀ along the pump axis, the z-axis in this case, which will cause the nuclear spins to precesses at their Larmor frequency ω_L about the z-axis, then applying a π/2 pulse with a frequency ω₀ equal to the ω_L of the isotope of interest on a perpendicular axis to the pump axis, the y-axis here. The pulse would abruptly deflect the magnetization vector of the nuclear spins to the xy-plane. A signal proportional to the nuclear spins as they re-align to the pump axis is detected along the y-axis, and an exponentially decaying sinusoidal wave was measured at a frequency equal to the Larmor frequency ω_L and a decay
D. Gas Content Measurement

Buffer and noble gasses contribute to the Rb transition line by broadening the light absorption spectrum and shifting the frequency of absorption by specific values for each gas, reported in [38] and [39]. The absorption data were fitted to a Voigt profile, which is a convolution between a Gaussian and Lorentzian functions, [40]. The Gaussian function accounts for Doppler broadening, while the Lorentzian function estimates broadening due to collisions with the buffer gas. An approximated Voigt profile is defined as, [40],

\[
F(x) = ax + b - \sum_{i=1}^{8} \left[ \frac{\eta}{x_i} \left( 1 + \left( \frac{x - x_i}{0.5 \Gamma_i} \right)^2 \right) \right] + (1 - \eta) \exp \left( \frac{x - x_i}{c \Gamma_i} \right)^2 ,
\]

where \(a\) and \(b\) are parameters of a line, \(c = 1/(2\sqrt{\ln 2})\), and \(\eta\) is the Lorentzian constant and its value is between 0 and 1. For each of the four ground transitions of \(^ {85}\text{Rb}\) and \(^ {87}\text{Rb}\), \(x_i\) is the center frequency of that transition in MHz, \(\Gamma_i\) is the Voigt width of that peak in MHz. The Voigt width is related to the Gaussian and the Lorentzian widths as follows, [41],

\[
\Gamma_V = 0.5346 \Gamma_L + \sqrt{0.2166 \Gamma_L^2 + \Gamma_G^2} ,
\]

where \(\Gamma_V, \Gamma_L, \Gamma_G\) are the Voigt, the Lorentzian, and the Gaussian widths, respectively.

The Rb dispenser that was used in our process consisted of a pure alkali metal and a getter material (SAES St 101). Once the dispenser is activated, the alkali metal is released, and the getter material absorbs active gasses, such as \(\text{O}_2, \text{H}_2, \text{CO}, \text{and N}_2\). To estimate the amount of remaining \(\text{N}_2\) gas, we filled an additional cell with 300 Torr of only \(\text{N}_2\) gas. We split a laser beam in half and passed the two beams, one through a reference cell with only natural Rb and the other through our fabricated cell, with Rb and other gasses. By sweeping the laser wavelength, we obtained two Rb light absorption spectrum curves, one for the reference cell, where the ground transitions of each isotope \(^ {85}\text{Rb}\) and \(^ {87}\text{Rb}\) can be distinguished, the other is for the fabricated cell, where these transitions are broadened and shifted due to the \(\text{N}_2\) gas, [38], [39]. Starting with the Rb light absorption spectrum of the reference cell and substituting for the broadening and frequency shift rates of \(\text{N}_2\) in an iterative curve fitting, we were able to find the \(\text{N}_2\) pressure that matched Rb light absorption spectrum curve of the fabricated sample. Fig. 12 shows the experimentally obtained Rb absorption curves for the reference cell, microcell with only Rb and \(\text{N}_2\), and the curve fit that satisfies the estimated \(\text{N}_2\) gas pressure inside the cell. We measured the \(\text{N}_2\) gas after two weeks of activation and found that the getter material in the Rb pill was saturated after absorbing 20% of the \(\text{N}_2\) gas, [42]. Note that this particular getter absorbs gasses at different rates. The relative sorption rates of \(\text{H}_2, \text{O}_2, \text{N}_2\) compared to \(\text{CO}\) are 50×, 6×, 0.5×, respectively, [43]. Absorbing other active gases faster than \(\text{N}_2\) ensures a clean environment inside the cell.

It should be noted that this method of estimating the gas inside the cell has uncertainty associated with the spin destruction cross-section between Rb and other gases, which affect the broadening and frequency shift constants. The spin destruction cross-section used in our curve fitting was adopted from [38] and [39].

E. Experimental Setup

The atomic cell was placed in a miniaturized oven made from a thermally insulating material, all housed by a nested 4-layer \(\mu\)-metal shield with integrated 3-axis magnetic field coils. The pump beam of 2.5mW with a circularly polarized light locked on Rb D1 line (795nm) along the z-axis. A DC field of 3.5\(\mu\)T and an RF field of 17.8kHz with an RMS amplitude of 3.5\(\mu\)T were applied along the z-axis. The probe beam was a linearly polarized beam of 1mW set off resonance from D2 line (780nm) and was applied along the y-axis. The produced RF signal was used as a reference for the lock-in amplifier that demodulated the output of the Faraday detector at the probe side (Faraday Detector is a balanced polarimeter used to detect Faraday Rotation). A \(\pi/2\) pulse at the frequency of the Xe isotope of interest was applied along the y-axis to obtain the FID signal, which was fitted to an exponentially decaying sine wave to extract the relaxation time \(T_2\). Fig. 14 shows an example of the FID signal for \(^ {131}\text{Xe}\) of PAXE01.

F. Coating

Alkali metals, like Rb, react with glass cells at elevated temperatures, which leads to a consumption of the metal. One method to reduce this interaction is by passivating the glass walls of the cells. In [44], it was shown that a 20nm layer of \(\text{Al}_2\text{O}_3\) can reduce the interaction between alkali metals and cell glass walls by 100×. It was also found that anodic bonding worked with ALD \(\text{Al}_2\text{O}_3\) as an intermediate layer.

ALD is a thin film conformal coating technique, the reaction of two chemicals in a gas phase with a surface creates one atomic layer, for example, Trimethylaluminum (TMA) and \(\text{H}_2\text{O}\) creates \(\text{Al}_2\text{O}_3\). The process is self-limiting to a single atomic layer per cycle. The coating is achieved by repeating
deposition cycles until the desired thickness is reached. In our study, we used a commercial ALD deposition system by Cambridge Nanotech to deposit 10 nm of Al₂O₃ on both samples and the capping wafer. The deposition parameters are summarized in Table III.

G. Results

Table IV summarizes the studied parameters and the average relaxation time of ²⁹Xe and ¹³¹Xe isotopes in the range from 115°C to 140°C. We observed that Atomic Layer Deposition (ALD) of 10 nm Al₂O₃ on the cell walls increased the transverse relaxation time of the ¹³¹Xe isotope by a factor of 3×, when compared to cells without coating. When using Aluminosilicate glass (ASG) instead of Borosilicate glass (Pyrex), we observed a similar effect on the relaxation time of ¹³¹Xe isotope, demonstrating an increase of T₂ by a factor of 2.5×. On the other hand, ALD coating of Al₂O₃ was found to reduce the relaxation time of the ¹²⁹Xe isotope by a factor of 2×, while the ASG glass did not show a significant difference in T₂ of ¹²⁹Xe, as shown in Table IV.

H. Discussion

Reduction of the relaxation time of the ¹²⁹Xe isotope in PAXE01 (ALD Al₂O₃ coated cell) is believed to be due to a magnetic field gradient inside the cell created by non-uniform pumping of Rb atoms. This pumping non-uniformity is a result of different beam bending angles as it transmits through the cell, which was discussed earlier in section IV. Vertical pumping and in-plane probing of the same sample showed an increase of relaxation time to 1.22s, which is on par with PXE01, and that supports our hypothesis.

To analyze improvements of the relaxation time constant of ¹²⁹Xe, we performed Fast Fourier Transform (FFT) to the FID signal of ¹³¹Xe of the three cells at temperature of 135°C. Subsequently, the FFT data were fitted with a triplet of Lorentzian functions. Table V summarizes the data fitting results. We observed two phenomena. The first observation is that the ALD Al₂O₃ coating and ASG glass suppressed quadrupole splitting by reducing the splitting frequency between the three peaks by 100× and 2.2×, respectively. The second observation is that ALD coating of Al₂O₃ and the use of ASG glass material reduced the width of the central peak by 3.2× and 2.5×, respectively. Fig. 15 shows FFT of FID signals of the three cells.

VI. CONCLUSION

We discussed different design considerations of micro-glassblown spherical cells for atomic sensors applications. These aspects included geometry, optical properties, material selection, and surface coating. We studied cell inner wall coating as well as cell glass materials. We found that 10nm ALD Al₂O₃ suppressed the quadrupole splitting of ¹³¹Xe by 100× and reduced the central frequency peak width by 3×, which corresponds to a 3× increase in the relaxation time. We also found that using ASG glass instead of Pyrex suppressed the quadrupole splitting of ¹³¹Xe by 2.2× and reduced the central frequency peak width by 2.5×, which corresponds to 2.5× increase in the relaxation time. We concluded that the ALD Al₂O₃ coating and the ASG glass did not have a significant impact on the T₂ of ¹²⁹Xe. In light of the experimental results and analytical models of NMRG ARW, [23], the NMRM fundamental sensitivity δBn, [10], and assuming the same SNR values, the Al₂O₃ coating is projected to reduce the NMRG ARW and NMRM δBn by more than threefold.

Although the scope and examples presented throughout the paper were focused on the atomic sensors applications, the design approach for producing highly spherical shells within the practical limits can be extended to other applications that utilize this fabrication technique. Examples of such applications include, but are not limited to, airflow [45], optical [21], [46], mechanical spherical resonators [47]–[49], and spherical shell gyroscopes [50].
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[31] ST 101 Non-Evaporable Getters


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